

## Electric Field Intensity Lesson Notes

### Focus Questions:

- What are the mathematical equations associated with the electric field intensity?
- How do you determine the direction of the electric field vector?

### Electric Field as Force per Charge

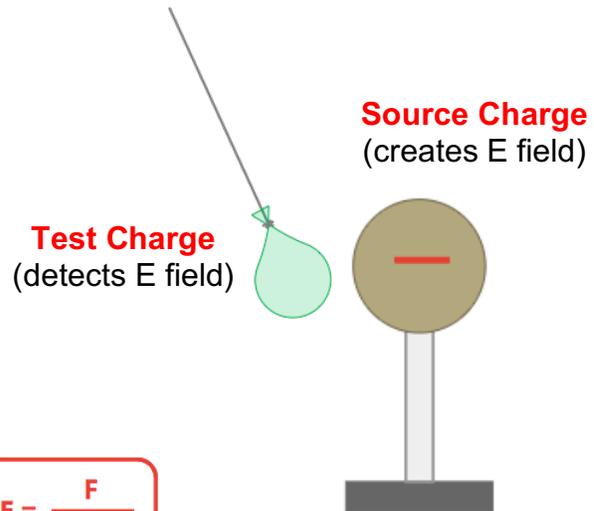
A charged object creates an electric field; we refer to it as the **source charge**.

To detect the presence of an electric field, a detector is required. We call the detector the **test charge**.

The strength of the electric field (**E**) at any given location is the amount of force per charge on the test charge.

$$\text{Electric Field} = \frac{\text{Force on Test Charge}}{\text{Charge on Test Charge}}$$

$$E = \frac{F}{q_{\text{test}}}$$



Unit on Electric Field: Newton/Coulomb, abbreviated N/C.

### Electric Field Does not Depend upon $q_{\text{test}}$

- Just because **E** is calculated as  $F/q_{\text{test}}$ , the value of electric field strength (**E**) does not depend on the quantity of charge on the test charge.
- Doubling  $q_{\text{test}}$  doubles the force; but the ratio of  $F/q_{\text{test}}$  remains the same.
- Tripling  $q_{\text{test}}$  triples the force; but the ratio of  $F/q_{\text{test}}$  remains the same.

### Derivation of a Second Electric Field Equation

$$E = \frac{F}{q_{\text{test}}} \quad \text{where ...} \quad F_{\text{elect}} = k \cdot \frac{Q_{\text{source}} \cdot q_{\text{test}}}{d^2}$$

$$E = \frac{k \cdot Q_{\text{source}} \cdot \cancel{q_{\text{test}}} / d^2}{\cancel{q_{\text{test}}}}$$

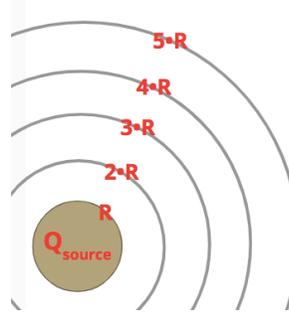
$$E = \frac{k \cdot Q_{\text{source}}}{d^2}$$

$$k = 9.0 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$$

## Inverse Square Law

There is an inverse square relationship between the electric field strength (**E**) and the distance of separation (**d**) from the source charge.

Doubling the distance from the source's center causes the E value to decrease by a factor of 4. Tripling the distance from the source's center causes the E value to decrease by a factor of 9. Etc.



|   | Distance | E (N/C) |
|---|----------|---------|
| 1 | R        | 800 000 |
| 2 | 2•R      | 200 000 |
| 3 | 3•R      | 89 000  |
| 4 | 4•R      | 50 000  |
| 5 | 5•R      | 32 000  |

## Two Equations for Electric Field

Equation expressing **E** in terms of how it is measured.

$$E = \frac{F}{q_{\text{test}}}$$

Equation expressing **E** in terms of the variables that affect it.

$$E = \frac{k \cdot Q_{\text{source}}}{d^2}$$

## Direction of Electric Field Vector

Electric field is a vector quantity and has a direction associated with it.

By definition, the direction of the electric field at any given location is the direction that a **+ test charge** would be pushed or pulled when placed at that location.

By logical extension, the electric field vector is directed ...

- towards negative source charges, and
- away from positive source charges.